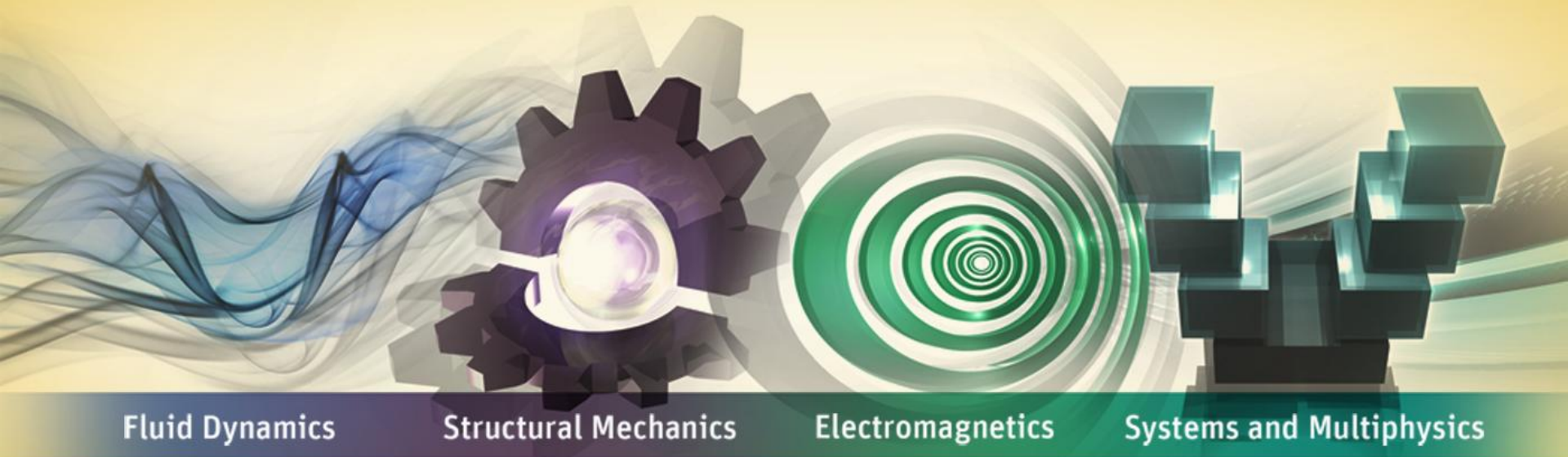


# Pseudo transient eye analysis by convolution method



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- In IBIS Asia summit 2008, we have first introduced statistical analysis method for GHz analysis

*<http://www.eda.org/ibis/summits/nov08a/li.pdf>*

- Statistical analysis used convolution method for fast SSE (Solution Space Explorer), but it has limits
  - Suitable for LTI system
  - Not as accurate as SPICE transient eye
- Today, we'll discuss the convolution method for Non-LTI system and introduce pseudo transient eye analysis by convolution method

# Convolution and LTI system

$$X_1(t) \Rightarrow Y_1(t)$$

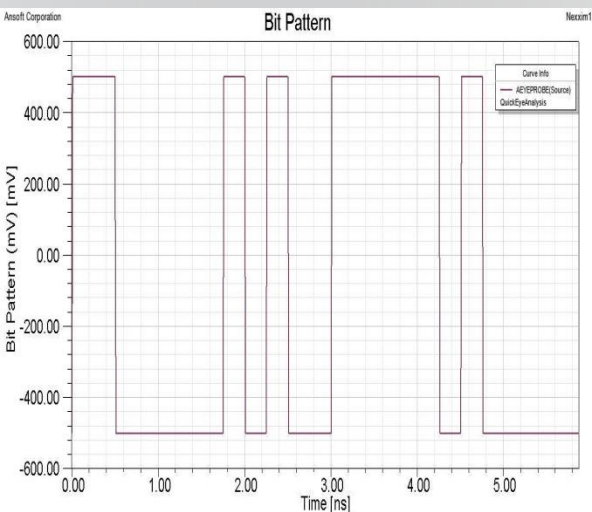
Input yields output

$$X_2(t) \Rightarrow Y_2(t)$$

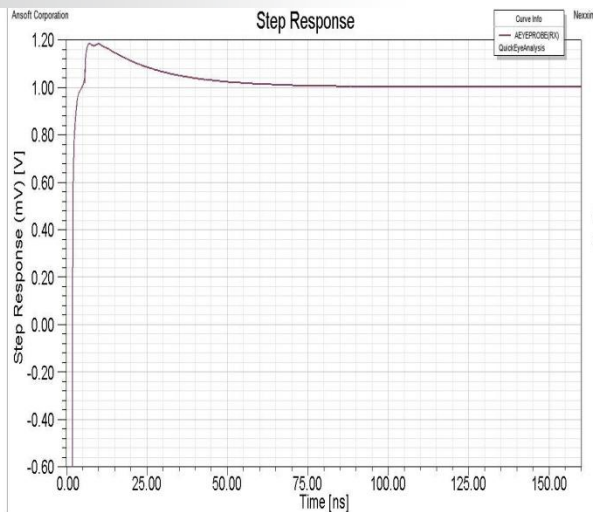
$$X_1(t) + X_2(t) \Rightarrow Y_1(t) + Y_2(t) \quad \text{Additive property}$$

$$aX_1(t) \Rightarrow aY_1(t) \quad \text{Homogeneity property}$$

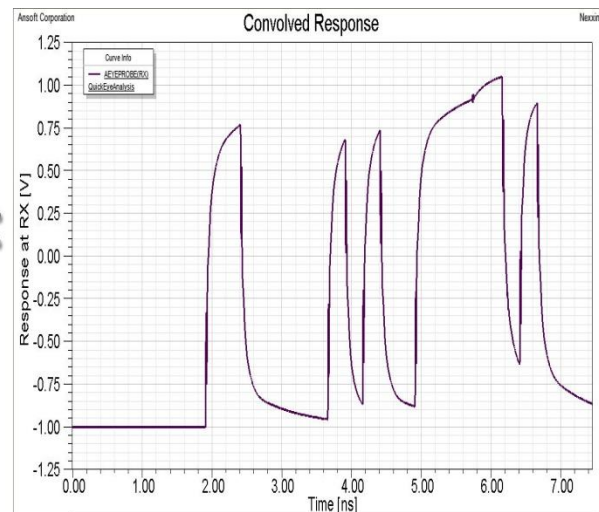
$$X_1(t - \tau) \Rightarrow Y_1(t - \tau) \quad \text{Time invariant property}$$



\*



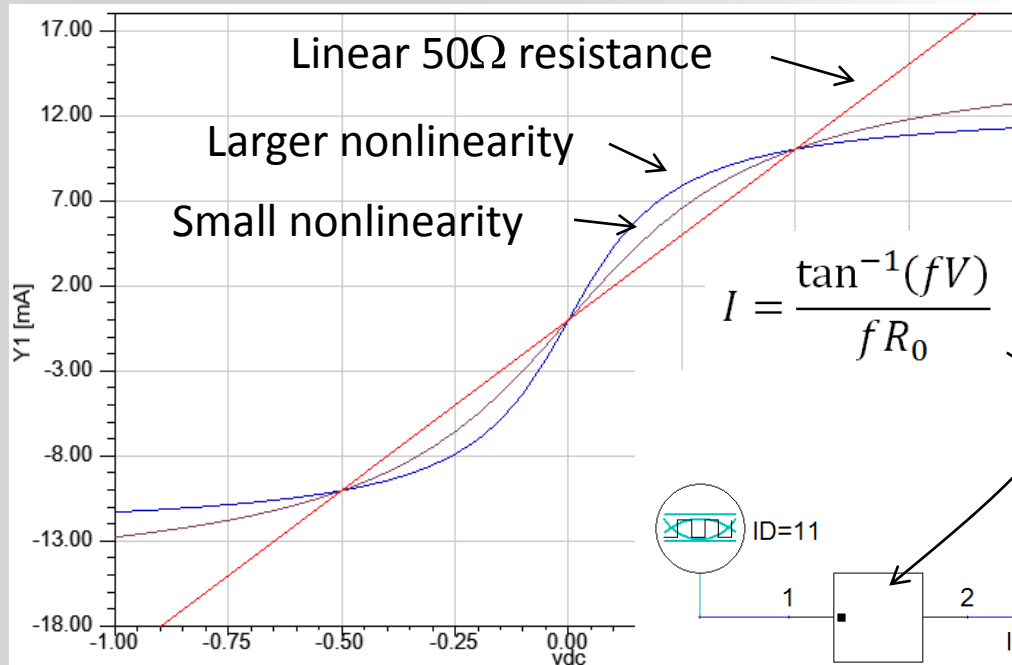
=



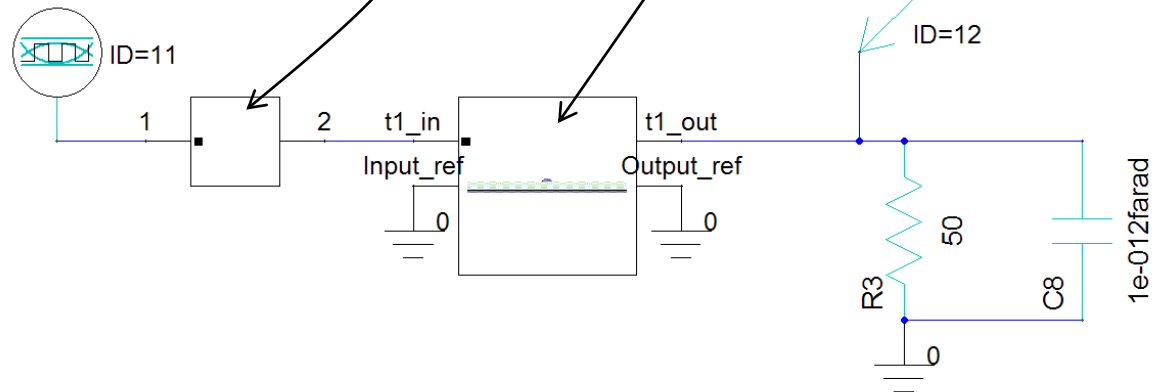
# How About Non-linear System?

Simple channel with driver that has a nonlinear self impedance:

- 3 curves tested for driver impedance



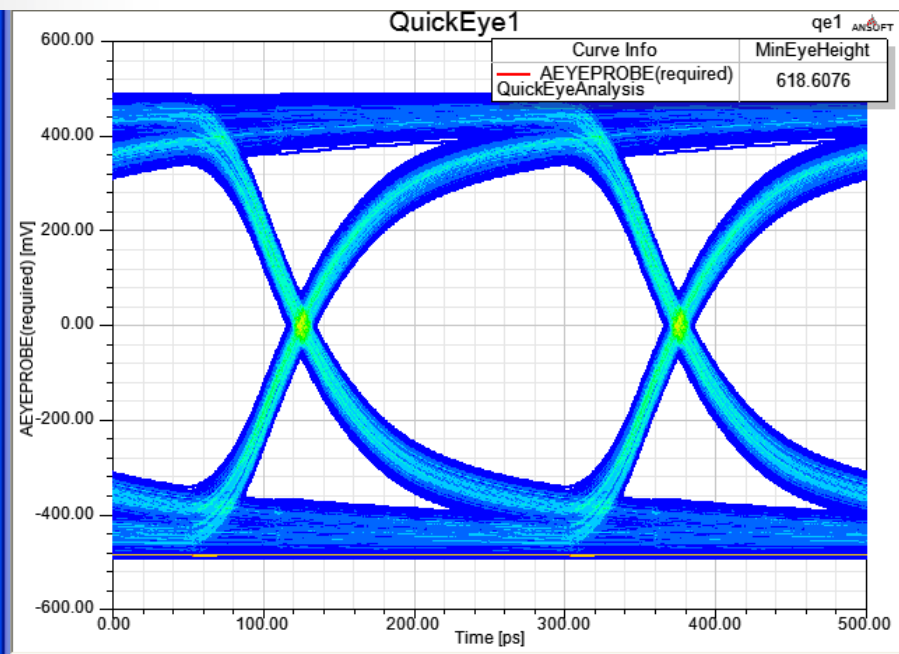
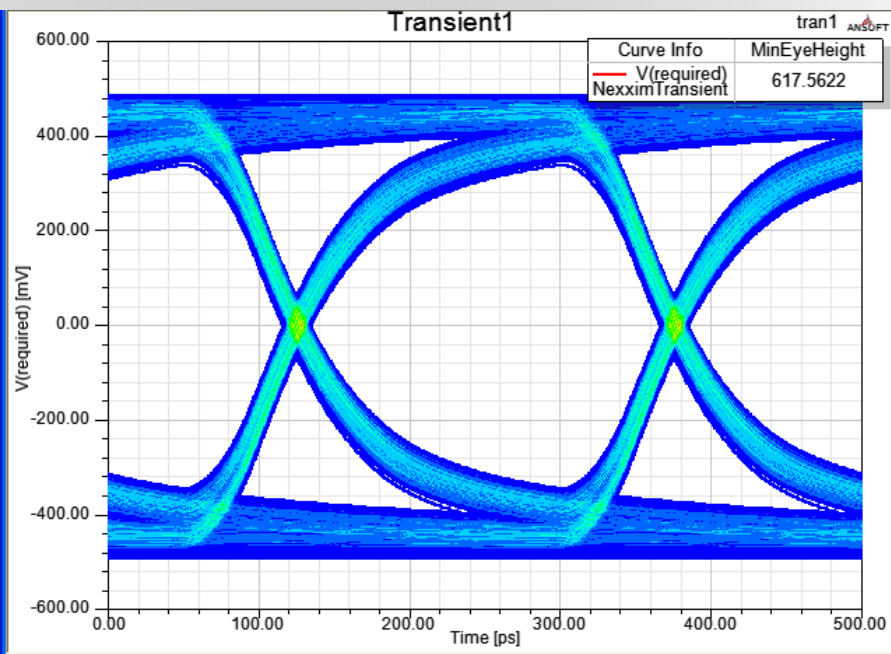
10 inch microstrip trace



# Transient vs. Convolution for Linear network

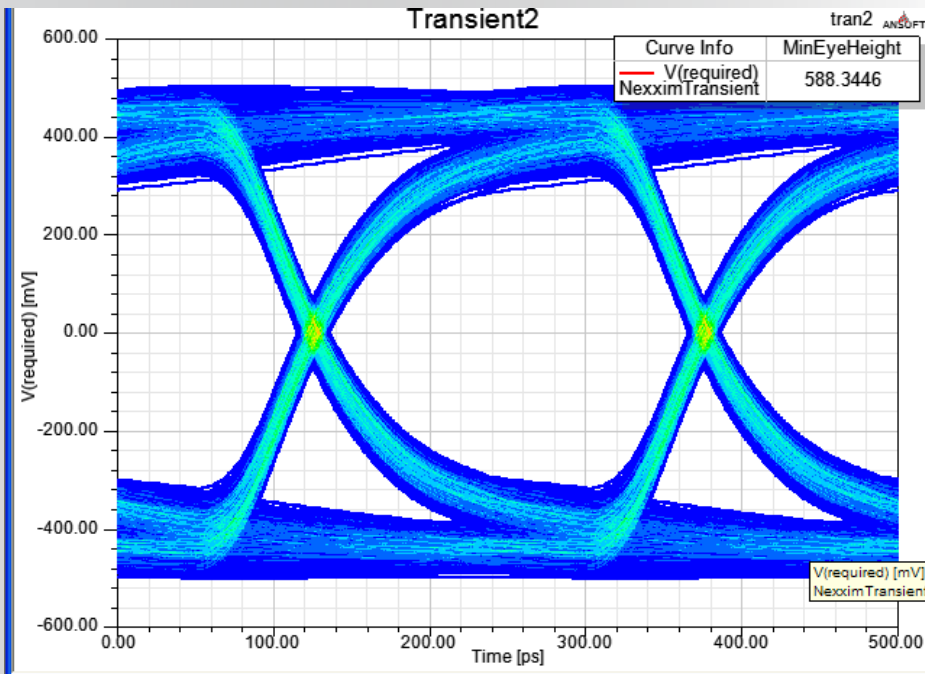
Transient Eye Height = 618 mV

Convolution Eye Height = 619 mV

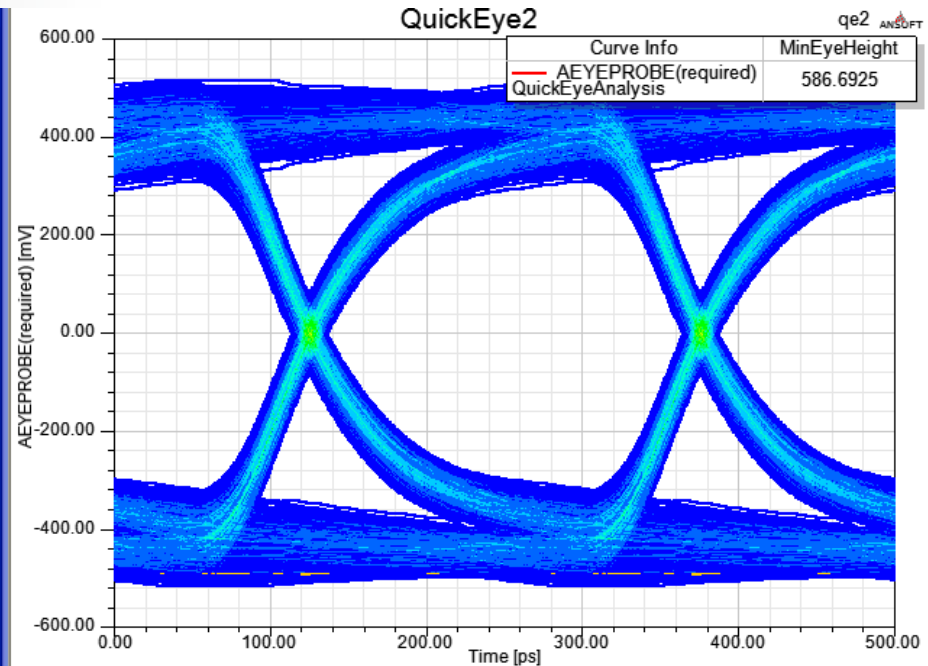


# Transient vs. Convolution for Small Nonlinearity

Transient Eye Height = 588 mV

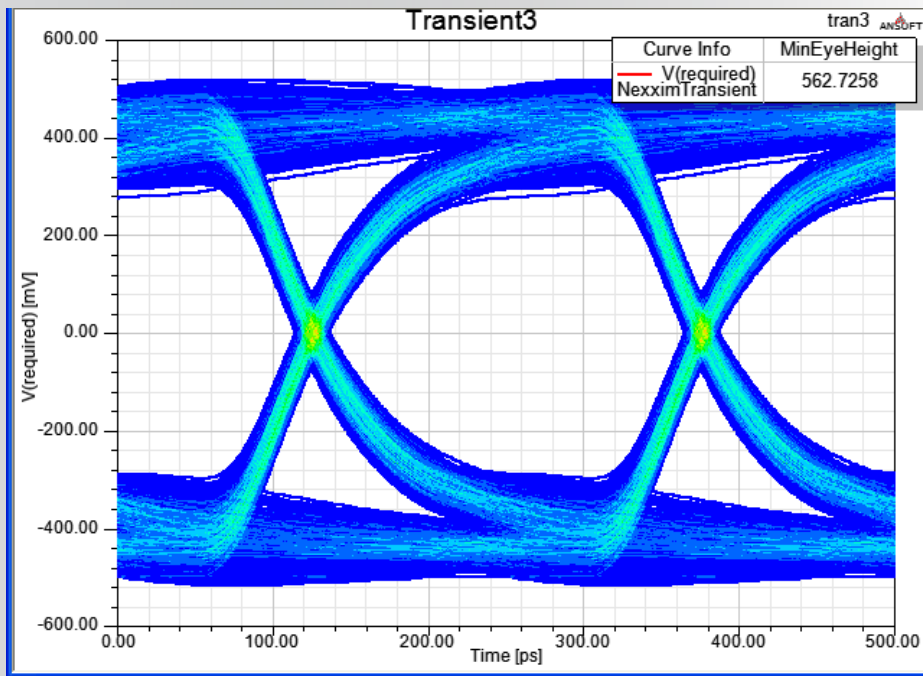


Convolution eye Height = 587 mV

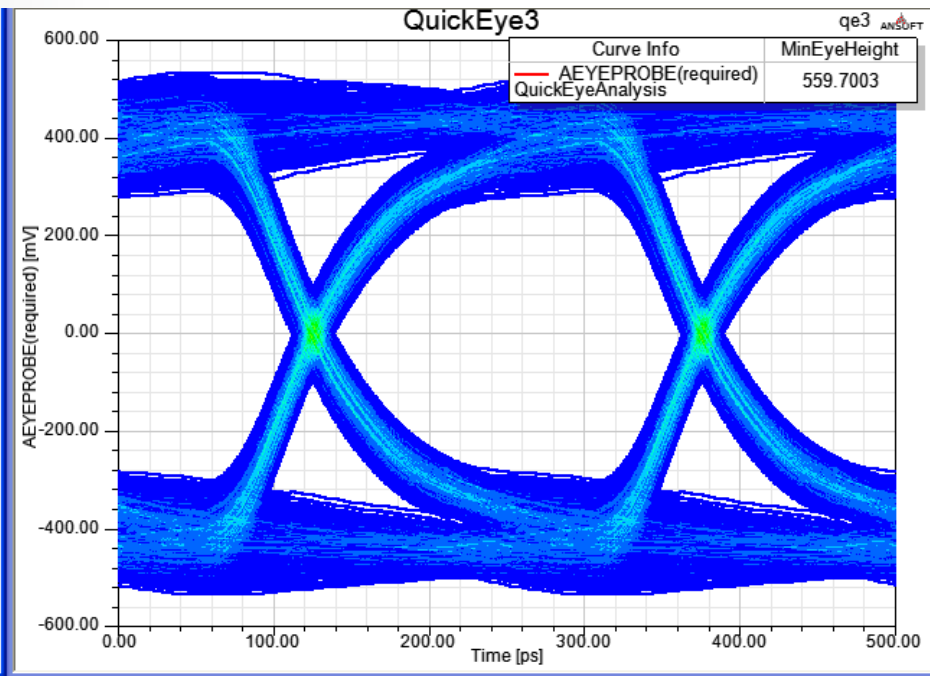


# Transient vs. Convolution for Larger Nonlinearity

Transient Eye Height = 563 mV



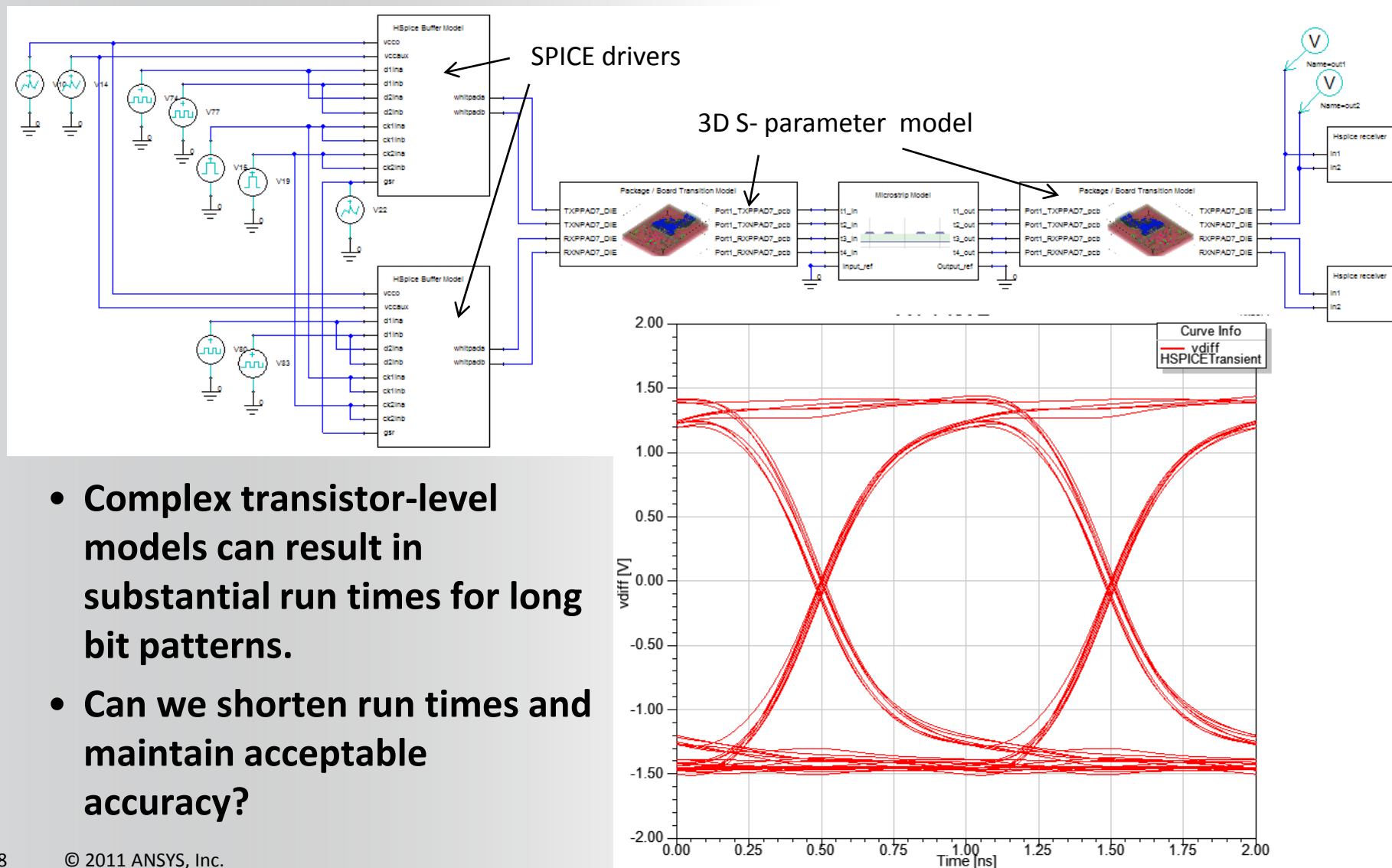
Convolution Height = 560 mV



- Test cases show that even Convolution make an assumption of linearity, accuracy is often excellent for moderately nonlinear drivers



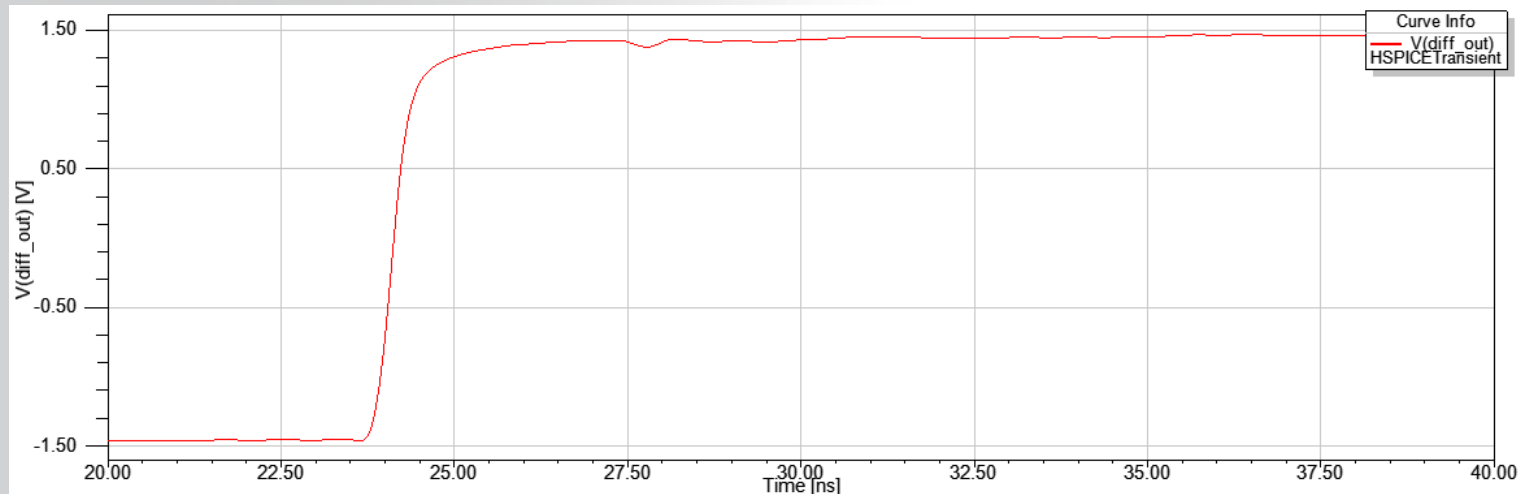
# Typical GHz Transient simulation





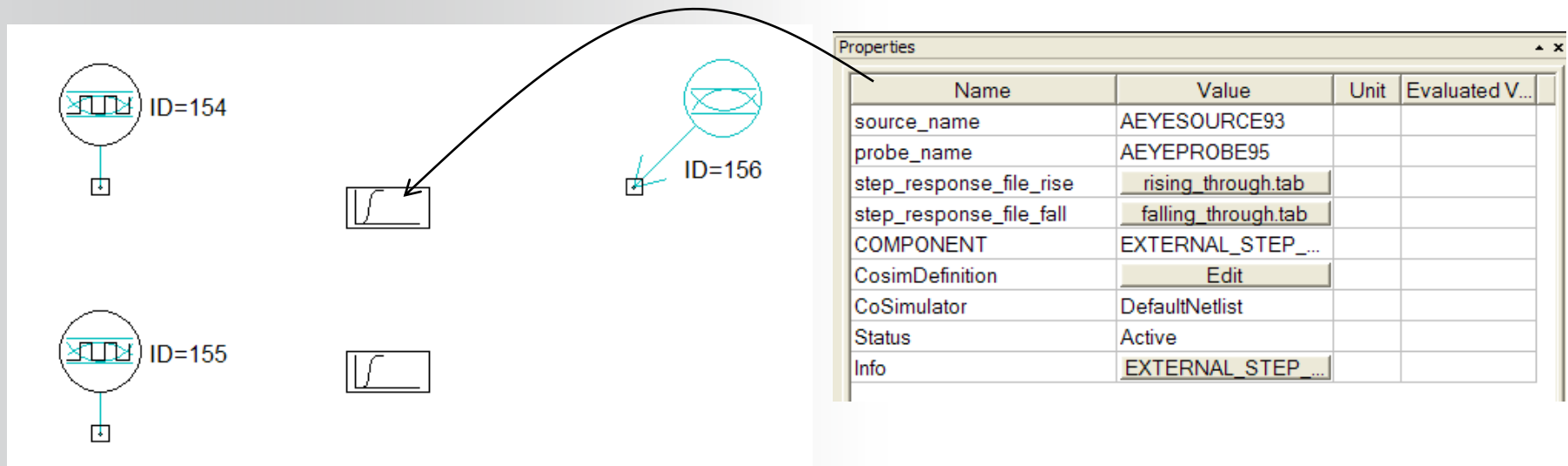
## Pseudo transient like IBIS' V-T curve:

- Run transient simulations using SPICE to capture the step response of the channel, Store step responses in text files
- Separate rising and falling responses can be specified
- Run convolution using these external step responses
- Theory is based on LTI assumption



# Pseudo transient eye analysis(cont.)

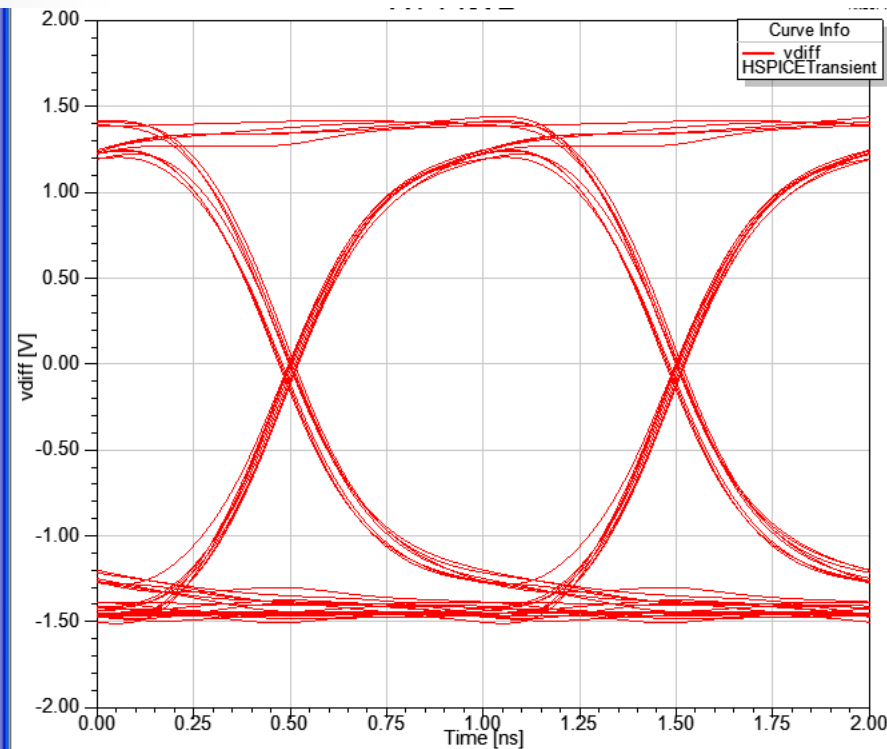
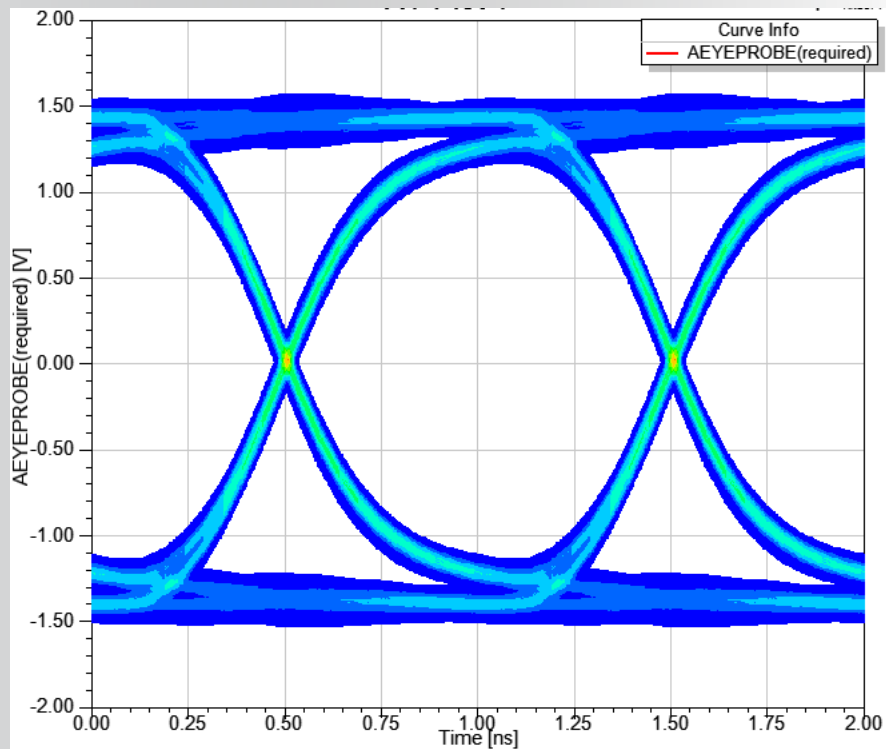
Pseudo transient eye results will closely match transient if buffers are approximately linear



# Pseudo transient eye vs. SPICE transient eye

## Pseudo transient and SPICE transient

- After capturing 100ns transient step response for rising, falling, and crosstalk edges, 100,000 bits run in seconds by convolution
- Results consistent with SPICE transient



- **Even Statistical eye analysis by using convolution method is assumption LTI system, sometimes it also can be used for Non-Linear system, but the simulator must be tested**
- **SPICE transient step response can also be used in Statistical analysis for Pseudo transient**
- **Chip vendor maybe supply typical channel's step response for end user evaluation. EDA vendor also can give the comparison of pseudo transient and SPICE transient for user reference.**